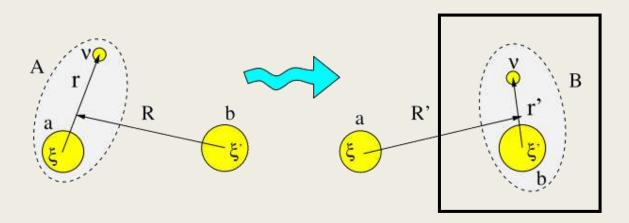
# Coupled-Channels Scattering Solutions using the R-matrix Method

**Ben Slimmer** 

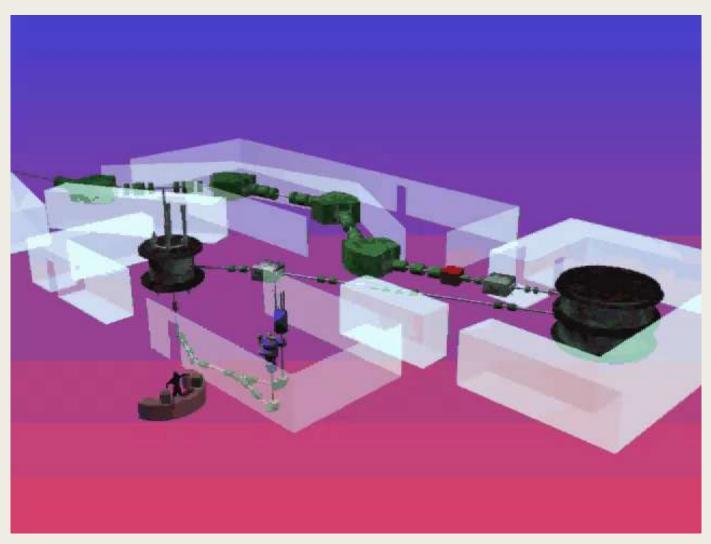
Collaborators: Joey Bonitati, Weichuan Li, Gregory Potel, Filomena Nunes

# Motivation

- Goal is to calculate wavefunctions for coupled channels scattering reactions with nonlocal interactions  $\left[-\frac{\hbar^2}{2\mu_c}\left(\frac{d^2}{dr^2} \frac{l_c(l_c+1)}{r^2}\right) + V_c(r) + E_c E\right] u_{c(c_0)}(r) + \sum_{c'} \int_0^\infty W_{cc'}(r, r') u_{c'(c_0)}(r') dr' = 0$
- R-matrix method offers an efficient framework for calculating such solutions.



# Context



### **R-matrix Method**

- Radial space the wavefunction will be solved for is divided at a channel radius
- Inside the channel radius, the wavefunction is calculated over a finite number of basis functions:

 $C_{ci,c'i'} = <\varphi_i | T_c + \mathcal{L}_c + E_c - E | \varphi_{i'} > \delta_{cc'} + <\varphi_i | V_{cc'} | \varphi_{i'} >$ 

In the exterior region, the asymptotic behavior of the wavefunction can be modeled using the collision matrix of the system and Coulomb functions<sup>[1]</sup>:

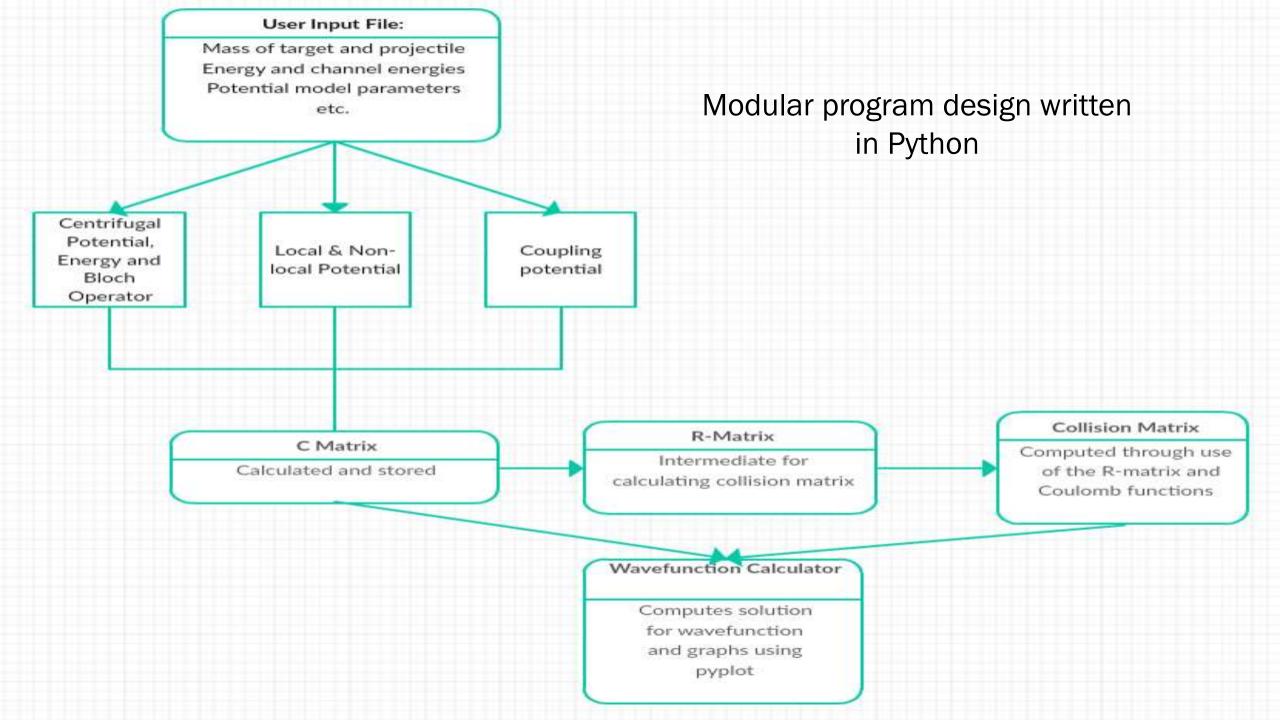
$$u_{c,ext} = v_c^{-1/2} (I_c(k_c r) \delta_{cc_0} - U_{cc_0} O_c(k_c r))$$

[1]: Descouvemont, P., & Baye, D. (2010). The R -matrix theory. *Reports on Progress in Physics*, 73(3), 036301.

#### Inputs

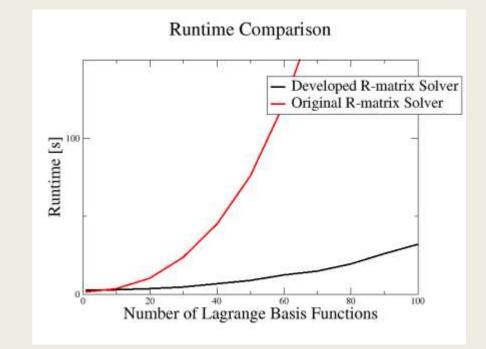
- Information about the system:
  - Energy of the incoming nucleon (E) and excitation energies  $(E_c)$
  - Angular momentum values (I)
  - Reduced mass of the system ( $\mu$ )
- Parameterization of potentials (V(r))
  - Both local and nonlocal
  - Model interaction between two particles in a channel and between the two coupled channels
  - Usual potential shape is of the Woods-Saxon form:  $V_{WS}(r) = \frac{-V_0}{r-R}$
  - Coupling potential model:

$$V_{coupling} = \beta_{coupling} \frac{d}{dr} \frac{V_c}{1 - e^{\frac{r - R_c}{a_c}}}$$



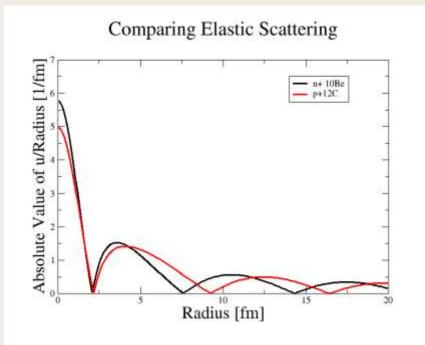
# **Program Development**

- Began with single channel R-matrix solver
- Generalized to calculate two coupled channel problems
- Optimized by performing as few matrix calculations as possible
- Large matrices calculated once and passed as parameters where needed



# **Preliminary Results**

Single-channel wavefunctions for elastic scattering: n+<sup>10</sup>Be E=5 MeV , p+<sup>12</sup>C both at 5 MeV.



Comparing with Fortran package<sup>[2]</sup>:  $n+^{10}Be$  at 5 MeV with  $E_c=3.368$  MeV (local coupled-channel case).

Coupled Channels Comparison

[2]:Descouvemont, P. (2016). An R-matrix package for coupled-channel problems in nuclear physics. *Computer Physics Communications*, 200, 199–219.

# **Future Improvements**

After more testing ensures the accuracy of the developed coupled channels solution, there are many opportunities for future work:

- Generalization for arbitrary number of channels
- Include parallel programming techniques.
- Expand the solver to three-body problems.

# Acknowledgments to iCER ACRES and NSCL